# Electrical Transport Properties of IrO<sub>2</sub> and RuO<sub>2</sub>†

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The electrical resistivities of single crystals of RuO2 and IrO2 in the temperature range 10-1000°K are reported. It is found that electron-phonon and electron-electron interband scattering mechanisms account quantitatively for the observed temperature dependence of the resistivities. The Hall constants measured at 300 and 77°K are also reported.

## I. INTRODUCTION

WE report here the temperature dependence and magnitude of the resistivities and the Hall constants of the oxides RuO2 and IrO2. These oxides, together with several other oxides of the fourth and fifth transition series, exhibit metallic conductivities in the range 0.01-1 times the conductivities of the parent metals themselves. Several of these oxides have been reported by Rogers et al.1 They include the oxides isoelectronic and isostructural to RuO2 and IrO2, which are  $OsO_2$  and  $RhO_2$ , respectively. Also the oxides,  $\alpha$ -, β-ReO<sub>2</sub>, WO<sub>2</sub>, and MoO<sub>2</sub> have been found to be metallic. The cubic oxide ReO<sub>3</sub> is also metallic, with a conductivity which is slightly higher than that of metallic Re.5

IrO<sub>2</sub> and RuO<sub>2</sub> crystallize in the rutile structure,  $D_{4h}^{14}$ , with two molecules per unit cell. Their lattice parameters are identical within 2%, being a=4.49 Å, c=3.11 Å for RuO<sub>2</sub>, <sup>6</sup> and a=4.51 Å and c=3.15 Å for IrO<sub>2</sub>. In this structure, the metal atoms, placed at the cell corner and body center, are very nearly octahedrally coordinated by oxygen atoms, with one axis of the octahedron being 4% shorter than the others. The electronic configuration for the cations, if the oxides are considered to be fully ionic, is  $4d^4$  for Ru and  $5d^5$  for Ir.

The determination of the intrinsic transport properties of oxides is often made difficult or impossible by surface properties or large defect concentrations which can dominate the transport properties or at least quickly mask intrinsic conduction mechanisms as the temperature is lowered. Work done on powdered oxides

is notorious for being inconsistent with bulk properties. We found, for example, that sintered pellets of IrO<sub>2</sub> did not give the correct order of magnitude or the correct temperature dependence of the conductivity. Similar results are found by comparing the work of Gibart<sup>3</sup> on powdered ReO<sub>2</sub> with that of Rogers et al. on crystals. Work on CrO<sub>2</sub> has also shown significant discrepancies between results obtained on powdered and singlecrystal samples.7

Even when single-crystal oxides can be obtained, they often have defect concentrations which make them unsuitable for a study of their intrinsic properties. Fortunately, the dioxides of iridium and ruthenium can be obtained as single crystals which are relatively defect-free. We have been able to measure the resistivity of these oxides in the temperature range 4.2-1000°K, and we have been able quantitatively to account for their observed temperature dependence above 10°K. We find that a relation based on electronelectron and electron-phonon interband scattering gives a good fit to our resistivity data. The same relation has been used to account for the behavior of some of the transition metals.8-10

In Sec. II we describe the sample preparation and experimental apparatus. In Sec. III the experimental results are given. The fit to the temperature dependence of the resistivity and a discussion of the physical significance of the various parameters used in the fit is given in Sec. IV.

## II. EXPERIMENTAL

# A. Sample Preparation

In growing single crystals of these materials, we make use of the fact that both metals have volatile oxide species which decompose to form the dioxide. This vapor-transport technique of crystal growth for these two oxides has been described previously by Schäfer

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et al.11 Briefly, the technique involves flowing O2 gas over the metal powder or metal oxide, the volatile species being transported in the gas stream down a temperature gradient until a point is reached where the volatile species decomposes forming the dioxide. Several crystal-growth habits were observed depending on the oxygen flow rate and temperature distribution. The orientations obtained in the case of  $IrO_2$  were  $\lceil 001 \rceil$ and [011] needles and (011) and (100) plates. The orientations obtained in the case of RuO<sub>2</sub> were [001] needles and (011) plates.

The vapor-transport technique of crystal growth provides a large measure of crystal purification. The deposition of IrO2 and RuO2 crystals was found to occur at very particular sites in the apparatus according to flow rate and temperature. Thus, for impurities to occur in the grown single crystals, they must have an appreciable vapor pressure or volatile carrier and must condense under the same conditions of gas flow and temperature as the host crystal. Of course, impurities may also enter through the growth substrate. Using magnetic-susceptibility data we have inferred that ferromagnetic impurity concentrations are less than 10 ppm. 12 Spectroscopic analysis has shown the presence of 10 ppm Si and 15 ppm Al in both the RuO2 and IrO2 as well as 100 ppm of Ca in the IrO<sub>2</sub>.13 The residualresistance ratio (RRR),  $R_{(300)}/R_{(4.2)}$ , may also be taken as a measure of sample perfection and was found to have values in the range 20-800. These ratios are not particularly high when compared with those obtained for pure metals. In view of the relatively high purity of our samples, the RRR which we obtain are probably attributable to lattice defects related to growth kinetics, rather than to foreign impurities, although we have not attempted a detailed study of this hypothesis.

The samples used for the transport measurements were taken as grown in most cases, although a few samples were cut to the desired orientation and shape by abrasion. The orientation of the crystals was determined by using a Laue back-reflection camera. The leads for the four-probe resistivity measurements and Hall-effect measurements were  $\frac{1}{2}$ - and 1-mil gold wires attached by thermal compression bonding. This involves heating the crystals to 400-500°C on the stage of a micromanipulator, placing the leads on the sample and crushing them with a 1×5-mil wedge using from 5×104-105 dyn of force. No strain could be detected in the region of the bond using Laue back-reflection photos. The sample dimensions were determined from photographic exposures at 500× and 75×, depending

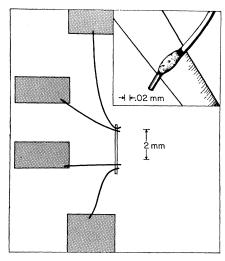


Fig. 1. IrO<sub>2</sub> c-axis needle is shown mounted with four electrical leads on an Al<sub>2</sub>O<sub>3</sub> substrate. The inset shows an enlargement of a 1-mil gold wire bonded to the crystal.

on sample size. In Fig. 1 an IrO2 needle is shown on its alumina substrate along with an enlargement of one of its thermal compression bond leads. The gold lead wires from the sample were compression-bonded to platinumgold islands on the Al<sub>2</sub>O<sub>3</sub> substrates.

# B. Apparatus

The resistance measurements were made using a four-probe technique. Both dc and ac measurements were made. The dc potentials were measured by means of a Leeds and Northrup type K-3 potentiometer. The ac potentials were obtained using a Princeton Applied Research type HR8 lock-in amplifier. Heating effects were noted in some samples, and in such cases the ac apparatus was used. This latter apparatus has a voltage sensitivity which is three orders of magnitude higher than the dc apparatus, and it thus allows the current levels to be 2-3 orders of magnitude lower than those needed for the dc measurements. Care was taken to insure that stray capacitive and inductive pickup was negligible.

The resistance measurements in the temperature range from 4-300°K were obtained using both a cryostat and by direct immersion in liquid helium and liquid nitrogen. The cryostat is of standard design and is described elsewhere.12 The temperature in this range was determined using a platinum resistance sensor (Rosemont Eng. Sensor H401) which was bonded along with the sample to an alumina chip by GE7031 varnish. Since the design of this sensor is somewhat nonstandard, it was calibrated against two other platinum resistors of more standard design.<sup>14</sup> These two calibrations agreed within ±0.2°K over the range 10-300°K. The

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<sup>&</sup>lt;sup>14</sup> We are indebted to B. Passenheim for the loan of these thermometers.

TABLE I. Resistivity of IrO<sub>2</sub> and RuO<sub>2</sub> determined at 300°K.

Crystal	Orientation	$ ho_{300}(\mu\Omega~{ m cm})$
IrO <sub>2</sub> : Ir6 Ir7 Ir22	[001] [001] [001]	$\begin{array}{c} 51.0 \\ 47.7 \\ 48.5 \\ \rho_{av}[001] = 49.1 \pm 0.5 \end{array}$
Ir14 Ir14' Ir25 Ir26	[011] [011] [011] [011]	31.9; 36.3 34.0 38.1 34.2 $\rho_{av}[011] = 34.9 \pm 1.0$
RuO <sub>2</sub> : Ru3 Ru4 Ru5 Ru11 Ru10 Ru14	~[111] [111] [011] [011] [100] [001]	$\begin{array}{c} 35.5 \\ 36.2 \\ 32.8 \\ 35.0 \\ 36.1 \\ 35.7 \\ \rho_{\rm av} = 35.2 \pm 0.5 \end{array}$

uncertainty in temperatures determined using the Rosemont sensor was then taken as  $\pm 0.2$ °K.

The electrical resistance measurements in the temperature range 300–1000°K were made with the sample in a tube furnace. The temperature in the sample tube was determined from a Pt-(Pt-10% Rh) thermocouple. This thermocouple was periodically checked against a Pt-(Pt-13% Rh) thermocouple which had a calibration, accurate to within 1°K, traceable to the National Bureau of Standards. The crystals had electrical lead wires connected as in the low-temperature measurements. The lead wires out of the furnace were gold and

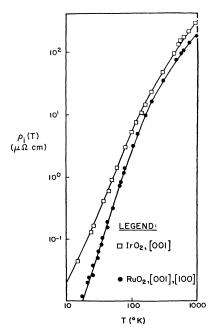


Fig. 2. Resistivity versus temperature of IrO<sub>2</sub> and RuO<sub>2</sub>. The solid lines are obtained from Eq. (4).

they were compression-bonded to the platinum-gold terminations of the alumina substrate.

The Hall voltage was measured using a Honeywell six-dial potentiometer and a Leeds and Northrup electronic null detector. This apparatus allowed the Hall voltage to be determined to  $\pm 5 \times 10^{-9}$  V. We estimate that our Hall measurements are accurate to  $\pm 10\%$  from the comparison of our results obtained for a polycrystalline copper sample and the previously reported Hall constants of copper.<sup>15</sup>

#### III. RESULTS

### A. Resistivity Magnitude

The resistivity tensor  $\tilde{\rho}$  in the principal-axis system for a tetragonal crystal structure is determined by the principal resistivities,  $\rho_c$  and  $\rho_a$ . For the case of IrO<sub>2</sub>, two different orientations were used to determine  $\rho_c$  and  $\rho_a$ , namely, [001] and [011]. Using the measured c-axis resistivity and the measured resistivity along [011], one finds

$$\rho_a = \frac{\rho \left[011\right] - \rho_c \sin^2 \varphi}{\cos^2 \varphi}; \quad \tan \varphi = c/a. \tag{1}$$

Seven IrO<sub>2</sub> samples were used in the determination of  $\tilde{\rho}$ , three c-axis samples and four [011] samples. The resistivities for these samples are listed in Table I. The average resistivity values at 300°K are  $\rho_c$ =49.1  $\mu\Omega$  cm and  $\rho_a$ =27.8  $\mu\Omega$  cm.

The resistivity was determined for six RuO<sub>2</sub> samples (see Table I) in four different orientations. All of the samples gave the same resistivity value, 35  $\mu\Omega$  cm, at 300°K to within experimental error. The main contribution to the uncertainty in resistivity values comes from determination of sample dimensions which in some cases may be irregular to 10% of a particular dimension. The values of  $\rho_c$  at 295°K reported earlier by Schäfer et al.<sup>11</sup> are 48  $\mu\Omega$  cm and 50  $\mu\Omega$  cm for IrO<sub>2</sub> and RuO<sub>2</sub>, respectively.

## B. Resistivity Temperature Dependence

In this section the temperature dependence of the resistivities of single crystals of RuO<sub>2</sub> and IrO<sub>2</sub> are reported. The resistivities were obtained from resistance measurements in the range 4.2 to 1000°K. We have obtained the intrinsic resistance ratios from the relation

$$R_i = \frac{R(T) - R(4.2)}{R(300) - R(4.2)},$$
(2)

where R(T) is the total resistance at temperature T. The values of  $R_i$  were scaled by the resistivity values given in Table I to obtain the temperature-dependent resistivities. The results are shown in Figs. 2-4. The

<sup>&</sup>lt;sup>15</sup> J. P. Jan, in *Solid State Physics*, edited by F. Seitz and D. Turnbull (Academic Press Inc., New York, 1957), Vol. 5, p. 45.

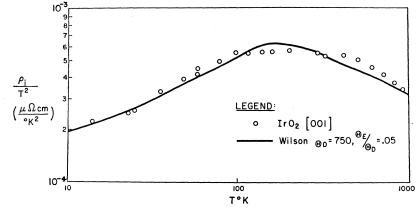


Fig. 3. Reduced resistivity  $\rho_i/T^2$  plotted as a function of T for a c-axis IrO<sub>2</sub> crystal.

solid lines of these figures are a theoretical fit discussed below in Sec. IV.

The open squares of Fig. 2 were obtained from one c-axis IrO<sub>2</sub> needle. The same data divided by  $T^2$  are shown in Fig. 3. Resistance ratios  $R_i$  were determined for a total of four IrO<sub>2</sub> crystals. Three of these were oriented along a [001] direction and the other was oriented along a [011] direction. The resistance ratios  $R_i$  of all of these samples showed the same temperature dependence to within experimental error down to  $10^{\circ}$ K. The residual resistance ratios, R(300)/R(4.2), are in the range 20–50 for all of these samples except one [001] needle. This latter sample had an RRR of 500.

The solid circles of Fig. 2 are data from three RuO<sub>2</sub> samples. Two of these samples were oriented with the current along [111] and the third sample was oriented with the current along [110]. In Fig. 4, the quantity  $\rho_i(T)/T^2$  is plotted versus T for sample Ru10. The resistance ratios  $R_i$  of six RuO<sub>2</sub> crystals were measured. These crystals were oriented along the [111], [011], [100], and [001] directions. The uncertainty in the data plotted in Figs. 3 and 4 has been determined from the instrumental uncertainty in determining  $R_i$  in Eq. (2) and from the temperature uncertainty. The uncertainty for the IrO2 data shown in Fig. 3 ranges from  $\pm 10\%$  at 10°K to  $\pm 3\%$  at 25°K. For the RuO<sub>2</sub> data shown in Fig. 4, this uncertainty is  $\pm 20\%$  at  $9^{\circ}$ K,  $\pm 10\%$  at 13°K,  $\pm 5\%$  at 16°K, and above 20°K it is negligible.

TABLE II. Hall constants and Hall mobilities of IrO<sub>2</sub> and RuO<sub>2</sub> determined at 300 and 77°K.

	Orientation		$R(10^4  \mathrm{cm}^3/\mathrm{A \; sec})$		$\mu(\text{cm}^2/\text{V sec})$	
	$\mathbf{H}$	J	300°K	77°K	300°K	77°K
RuO <sub>2</sub>	⊥ (011) ⊥ (011) ⊥ (011)	[011] [100] [111]	-1.1 $-1.2$ $-1.0$	-0.79 -0.90 -0.75	3.1 3.4 2.8	61 67 55
${ m IrO_2}$	[100] ⊥(0Ĭ1)	[001] [011]	$+3.58 \\ -2.60$	$+4.70 \\ -3.12$	7.3 7.5	120 130

### C. Hall Effect

The Hall constants at 300 and 77°K have been determined for two IrO<sub>2</sub> crystals and three RuO<sub>2</sub> crystals. The values are listed in Table II. The values for RuO<sub>2</sub> are isotropic to within  $\pm 10\%$  and their sign indicates that electrons have the predominant mobility. The Hall constants of IrO<sub>2</sub> crystals show both electron-like and holelike behavior. For current directed along the c axis the Hall constant is positive and for current along [011] the Hall constant is negative. The Hall mobilities, taken simply as  $\mu_H = R_H/\rho$ , are listed in Table II.

### IV. DISCUSSION

One of the major objectives of this work is to determine the scattering mechanisms which give the dominant contribution to the resistivity of pure RuO<sub>2</sub> and IrO<sub>2</sub>. In principle, the temperature dependence of the electrical resistivity can be used to determine the conduction-electron scattering mechanism(s) (CESM) occurring in a particular metal. In fact, such a program

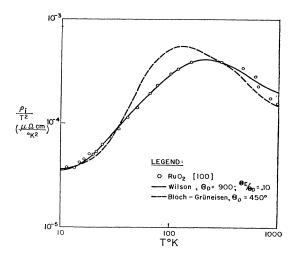


Fig. 4. Reduced resistivity  $\rho_i/T^2$  plotted as a function of T for an a-axis RuO<sub>2</sub> crystal.

may give ambiguous results since it may occur that two or more CESM have nearly the same temperature dependence so that they cannot be distinguished in the available temperature range. It may also happen that there are deviations from Matthiessen's rule which give an additional temperature dependence apart from those of the intrinsic scattering mechanisms. 16,17 Although these difficulties have arisen in our analysis of  $\rho_i(T)$  for these two oxides, we have been able to fit a relation based on two interband scattering mechanisms to the measured resistivities in the temperature range 10-1000°K.

In general, the resistivity of an isotropic metal can be written in the form

$$\rho(T) = \rho_0 + \rho_i(T) + \Delta(T), \qquad (3)$$

where  $\rho_0$  is the total resistivity at T=0°K and is independent of temperature,  $\rho_i(T)$  is the intrinsic resistivity of the defect-free metal, and  $\Delta(T)$  is a temperature-dependent term arising from the nonadditivity of  $\rho_0$  and  $\rho_i(T)$ . The generalization of Eq. (3) to anisotropic metals could be quite complex. However, we find for these tetragonal crystals that the ratio  $\rho_{ic}(T)/\rho_{ia}(T)$  is independent of temperature. It is then possible to make a single fit, except for a temperature-independent factor, to the two components of  $\tilde{\rho}_i$ .

The temperature dependence of  $\rho_i$  expected for various scattering mechanisms has been reviewed by Ziman<sup>18</sup> and by Wilson.<sup>8</sup> The roughly  $T^2$  and  $T^3$  temperature dependences of the resistivities which we have found for IrO2 and RuO2 are typical of some of the transition metals. <sup>19</sup> In particular, the  $T^2$  and  $T^3$  dependences of the resistivity of Pt and Pd below 30°K were shown originally by Baber<sup>9</sup> and Wilson<sup>8</sup> to be accounted for by electron-electron and electron-phonon interband scattering, respectively. These treatments followed Mott's proposal that the higher density of states and effective masses of the d-band holes would allow this band to act as a "trap" for the more mobile s-band conduction electrons.<sup>20</sup> These early treatments of interband scattering do not rely on the s or d character of the bands, but rather on the condition that there be an appreciable difference in the effective masses of these bands. It is not obvious that such a condition can be met in these oxides. It is usually assumed that the d bands contribute only low mobility carriers to conduction processes. However, in these compounds, highmobility carriers may arise from the d-band manifold itself if appreciable hybridization with the oxygen p bands occurs. Although detailed energy-band calculations are not as yet available for RuO<sub>2</sub> and IrO<sub>2</sub>, the recent calculation by Mattheiss<sup>21</sup> for ReO<sub>3</sub> illustrates the extent of p-d hybridization for this latter oxide. He finds that the width of the  $t_{2g}$  d manifold,  $\sim 4$  eV, arises almost entirely from p-d hybridization. In general, this hybridization may vary considerably over the Brillouin zone depending on the details of the symmetry of the bands within the p and d manifolds. Thus it is reasonable to expect the Fermi surface to consist of several sheets having widely varying effective masses. In view of the observed temperature dependence of the resistivity of these oxides and the possible nature of the d bands as given above it is reasonable to try to account for the observed resistivity via the scattering mechanisms discussed by Baber<sup>9</sup> and by Wilson.<sup>8</sup>

The treatments of Baber<sup>9</sup> and Wilson,<sup>8</sup> when taken together, require  $\rho_i$  to be given by a relation of the form

$$\rho_i(T) = \rho_2 T^2 + \rho_3 T^3 [J_3(\Theta_D/T) - J_3(\Theta_E/T)],$$
 (4)

where T is the absolute temperature,  $\Theta_{\rm D}$  is the usual Debye temperature, and  $\Theta_{\mathbf{E}}$  is a parameter characterizing the momentum gap between heavy- and lightmass bands. The function  $J_3$  is a standard transport integral and has been tabulated. 10 The magnitude of the  $T^2$  term is  $\rho_2$  and the parameter  $\rho_3$  is used to normalize Eq. (4) to the measured resistivity at 300°K. The contribution to the electrical resistivity from electronelectron interband scattering has been discussed more recently by Ziman,18 Appel,22 and Rice.23 The second term on the right of Eq. (4), derived by Wilson, has been discussed recently by Colquitt10 for the case of the transition metals.

The solid lines of Fig. 2 represent Eq. (4). The choice of the parameters in fitting the data to Eq. (4) is facilitated by the fact that each of the parameters  $\rho_2$ ,  $\Theta_{\rm D}$ , and  $\Theta_{\rm E}$  dominate the temperature dependence over a particular temperature range. Thus  $\rho_2$  is chosen to fit the resistivity in the range 10-20°K, where the electronphonon term is small, and  $\Theta_{\rm D}$  is chosen to fit the resistivity in the temperature range above 100°K, where the fit is independent of  $\rho_2$  and  $\Theta_E$ . In the intermediate temperature range the parameter  $\Theta_{\rm E}$  can be chosen independently of  $\Theta_D$  since in that range the function  $J_3(\Theta_D/T)$  has a strictly  $T^3$  dependence for a wide choice of  $\Theta_D$ . This procedure requires that  $\Theta_D/T \gtrsim 10$  in the intermediate temperature range.

The parameters required to fit Eq. (4) to the measured values of  $\rho_i(T)$  are significantly different for the two oxides. The most striking difference between the parameters for the two oxides is the magnitude of the electron-electron term, it being ten times larger in the case of IrO<sub>2</sub>. The uncertainty in the choice of electronphonon parameters is larger in the case of IrO<sub>2</sub> than for RuO<sub>2</sub>. The parameters and their uncertainty are indicated in Table III. The fit can be more clearly displayed

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Table III. Parameters of Eq. (4) as determined from the measured resistivities of IrO<sub>2</sub> and RuO<sub>2</sub>.

	$^{ ho_2}_{(10^{-5}} \ _{\mu\Omega\ { m cm/°K^2})}$	$ ho_3 \ (10^{-7} \ \mu\Omega \ { m cm/°K^3})$	$\Theta_{\mathrm{D}}(\mathrm{^{\circ}K})$	$\Theta_{ m E}/\Theta_{ m D}$
RuO <sub>2</sub>	3.5±0.5	3.2	$900\pm 50$	$0.1 \pm 0.02 \\ \sim 0.05$
IrO <sub>2</sub>	17.7±0.8	5.56	$700\pm 100$	

by dividing out the  $T^2$  dependence in Eq. (4). A plot of  $\rho_i/T^2$  versus T is shown in Figs. 3 and 4 for IrO<sub>2</sub> and RuO<sub>2</sub>, respectively.

Several alternatives to Eq. (4) were tried. However, no improvements in the fit listed in Table III could be obtained. The best fit which uses a strictly Bloch-Gruneisen formula also is shown in Fig. 4.

In fitting  $\rho_i$  in Eq. (4) to the measured resistance ratios given by Eq. (3), we have assumed that Mattheissen's rule is valid. This assumption is justified if it is found that  $R_i$  in Eq. (2) is the same for samples having different RRR. In the case of IrO2 this condition was found to be valid for our crystals, which had RRR in the range 20-500. In the case of RuO<sub>2</sub> it was difficult to establish the dependence of  $R_i$  on RRR since most of the samples had the same RRR. One RuO<sub>2</sub> sample which appeared "erroded" had a RRR which was 10× less than the other RuO<sub>2</sub> samples and deviations from Matthiessen's rule were found. Although the behavior of this sample may not be typical of lower RRR samples, we have used it to estimate an upper limit on the possible deviations from Matthiessen's rule for RuO<sub>2</sub>. These upper limits are found to be 30% at 20°K, 15% at 30°K, 7% at 40°K, and 3% at 60°K. These uncertainties do not affect the choice of  $\Theta_D$ , but they are the major source of uncertainty in  $\Theta_{\rm E}$  and  $\rho_{\rm 2}$ .

For these oxides the magnitude of the  $T^2$  term,  $\rho_2$ , of Eq. (4) which we find is comparable to those of some of the transition metals. A few of these values are as follows: (in units of  $10^{-5} \mu\Omega$  cm/°K<sup>2</sup>) Pd, 3.3; Pt, 14; Mn, 15 000; (19); and IrO<sub>2</sub>, 18; RuO<sub>2</sub>, 3.5. The physical significance of the magnitude of the  $T^2$  term in Eq. (4) is not clear since several scattering mechanisms have a  $T^2$  temperature dependence. Besides the scattering of electrons by a screened Coulomb interaction, discussed by Baber, the scattering of s-band conduction electrons by fluctuations in the uniform spin density of the d band via an exchange interaction also gives a  $T^2$  temperature dependence. This latter mechanism has been the subject of more recent work treating the low-temperature resistivity of Pd and Pd-Ni alloys.24 In any case, independent determinations of the parameters of the Fermi surface such as the Fermi energy and the band effective masses as well as screening lengths would be required before detailed comparisons between theoretical expressions and measured values of  $\rho_2$  could be made. This information is, for the most part, unknown.

The temperature dependence of the resistivity given by the Wilson term in Eq. (4) can be summarized as follows. At high temperature the resistivity is a linear function of temperature. At temperature below  $\Theta_{\rm D}/5$  the resistivity varies as  $T^3$  and as the temperature is lowered still further the resistivity varies ultimately as  $e^{-\Theta_{\rm E}/T}$  for  $T < \Theta_{\rm E}/5$ . The T and  $T^3$  dependence has often been observed. However, the ultimate exponential dependence has never been unambiguously observed.

The difficulty in observing this latter behavior lies in the fact that the type of metal which exhibits electronphonon interband scattering also exhibits electronelectron scattering. The magnitude of the resistivity attributed to the latter scattering mechanism dominates the total resistivity in the temperature range where the exponential dependence should appear. Considering typical residual resistivities, we find that it is then necessary to resolve the total resistance to parts in  $10^3-10^5$  in order to see the phonon resistivity.

Up to this point in our discussion, we have neglected the possibility that the interband contribution to the resistivity becomes equal to the intraband contribution. If this occurs at temperatures above the exponential region of the Wilson formula, then this latter region will in principle be unobservable. In any case, the parameter  $\Theta_{\rm E}$  can be evaluated in a temperature range above that required to see the exponential behavior since the resistivity decreases significantly faster than  $T^3$  in the range  $T < \Theta_E$ . In the case of Pt and Pd, the values of  $\Theta_{\rm E}$  obtained from resistivity measurements are in good agreement with those estimated from the empirically determined Fermi surface.<sup>25</sup> Although the parameter  $\Theta_{\rm E}$  can, in principle, be calculated using the sound velocity and Fermi-surface dimensions, 25 neither the sound velocities nor enough detailed information about the Fermi surfaces of these oxides is known to allow such an estimate to be made.

In the case of RuO<sub>2</sub> it is interesting to see to what extent the electron-phonon resistivity approaches the exponential region predicted by Wilson. In Fig. 5 we plot the Wilson term in Eq. (4) versus  $\Theta_{\rm E}/T$  in the temperature range  $T<\Theta_{\rm E}$ . For  $\Theta_{\rm E}=90^{\circ}{\rm K}$ , the Wilson term in Eq. (4) becomes strictly exponential (the dashed line of Fig. 5) below 10°K. The open circles of Fig. 5 are the data points for sample Ru10 with the term  $\rho_2 T^2$  in Eq. (4) subtracted. In plotting these data, no account has been taken of the possible deviations from Matthiessen's rule discussed above. For this reason, the conclusion that the exponential region may be observable in RuO<sub>2</sub> is unreliable. Further measurements on higher RRR samples in the region extending below 10°K are required.

The values of the Debye temperature we obtain for IrO<sub>2</sub> and RuO<sub>2</sub> by fitting the Wilson term in Eq. (4) in the region 100–300°K are some 50% higher than the values obtained by Passenheim from specific-heat

<sup>&</sup>lt;sup>24</sup> A. I. Schindler and M. J. Rice, Phys. Rev. 164, 759 (1967).

<sup>&</sup>lt;sup>25</sup> W. D. Ryden, Solid State Commun. 6, 847 (1968).

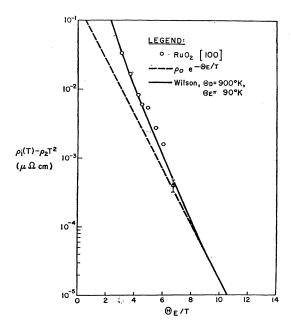


Fig. 5. Wilson term in Eq. (4) is plotted versus  $\Theta_E/T$  showing the exponential behavior expected for this term at the lowest temperatures.

measurements. For the purposes of this discussion we label the resistivity Debye temperatures  $\Theta_{\rm R}$ , and the specific-heat Debye temperatures  $\Theta_{D}$ . The values of Θ<sub>D</sub> for RuO<sub>2</sub> and IrO<sub>2</sub> were obtained from the coefficient of the  $T^3$  term of the specific heat in the region 0.5-10°K.13 In general, for the monovalent metals, the agreement between  $\Theta_R$  and  $\Theta_D$  is much better than that reported here for RuO2 and IrO2. Blackman26 has pointed out that the agreement between  $\Theta_R$  and  $\Theta_{\rm D}$  for many metals is fortuitous considering the assumed lattice models. He argues that, since the formulation of the resistivity assumes only the presence of longitudinal lattice vibrations while the specific heat includes both longitudinal and transverse vibrational modes, the two parameters should differ. He calculates the Debye temperature for Al and W from the average longitudinal sound velocity and compares it with a similar calculation including both longitudinal and transverse modes. He finds for aluminum,  $\Theta_L = 707^{\circ} \text{K}$ and  $\Theta_D = 415^{\circ} K$ , and for tungsten,  $\Theta_L = 636^{\circ} K$  and  $\Theta_{\rm D} = 384$ °K. These calculated differences between  $\Theta_{\rm L}$ and  $\Theta_{\rm D}$  are similar to those between  $\Theta_{\rm R}$  and  $\Theta_{\rm D}$ determined for RuO<sub>2</sub> and IrO<sub>2</sub>. This suggests that only longitudinal lattice vibrations are effective in scattering electrons for these two oxides. In the case of the monovalent metals, particularly the noble metals, it has been argued by Ziman<sup>18</sup> that both longitudinal and shear waves scatter electrons equally and would thus account for the agreement of  $\Theta_R$  and  $\Theta_D$  in those metals. Although the above argument for these oxides may be correct, it requires that shear waves be ineffective in scattering electrons in these oxides, and this supposition is not obvious.

It is found that both  $\Theta_R$  and  $\Theta_D$  for  $RuO_2$  and  $IrO_2$  nearly scale as

$$\frac{\Theta_D(\text{RuO}_2)}{\Theta_D(\text{IrO}_2)} = \left[\frac{M(\text{IrO}_2)}{M(\text{RuO}_2)}\right]^{1/2} = 1.3,$$
 (5)

where M is the molecular weight of the dioxide molecule. We find from resistivity measurements  $\Theta_{\mathbb{R}}(\mathrm{RuO_2})/\Theta_{\mathbb{R}}(\mathrm{IrO_2})=1.3$ , and Passenheim and McCollum<sup>13</sup> find from specific-heat measurements  $\Theta_{\mathbb{D}}(\mathrm{RuO_2})/\Theta_{\mathbb{D}}(\mathrm{IrO_2})=1.35$ . If the elastic constants of these two oxides are the same, then a relation of the form of Eq. (5) follows from a Debye model of a solid composed of dioxide molecules. This relation should hold regardless of the contribution of the longitudinal and transverse phonons to  $\Theta_{\mathbb{R}}$  and  $\Theta_{\mathbb{D}}$ .

The interband nature of the scattering mechanisms discussed here implies that the Fermi surfaces of these oxides consists of several sheets of quite different effective-mass carriers. In the case of RuO<sub>2</sub> this has to some extent been confirmed. Both the de Haas-van Alphen measurements of Marcus and Butler<sup>27</sup> and the magnetothermal oscillation measurements of Graebner and Ryden<sup>28</sup> have confirmed a Fermi surface consisting of at least two sheets of appreciably different mass carriers.

<sup>&</sup>lt;sup>26</sup> M. Blackman, Proc. Phys. Soc. (London) A64, 681 (1951).

S. M. Marcus and S. R. Butler, Phys. Letters 26A, 518 (1968)
 J. E. Graebner and W. D. Ryden (unpublished).